

# Translation from Workflow Nets to MSVL<sup>\*</sup>

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**Abstract.** An automatic translation from Workflow nets (WFNs) to Modeling, Simulation and Verification Language (MSVL) is presented in this paper. As a result, WFNs can be simulated and verified through the well developed supporting tool named MSV for MSVL programs. To do so, annotations are added to WFNs first. Further, translating rules are presented w.r.t regular structures for the translation from Annotated WFNs to MSVL programs. Finally, a tool called PN2MSVL has been implemented for the automatic translation from WFNs to MSVL.

**Keywords:** Workflow Nets, MSVL, Modeling, Verification, Simulation.

## 1 Introduction

As a subset of Petri nets [16], Workflow Nets (WFNs) [1] have been widely adopted in modeling business processes. WFNs combine an intuitive graphical formalism with a mathematical sound foundation. The graphical representation is useful in capturing the intuition of a modeler faithfully while the formal foundation allows the verification of a variety of properties [8, 16]. However, as an abstract model, WFNs are not implementable although some tools, e.g. CPN [4], can support the simulation and verification of WFNs.

To implement WFNs, several transformations from WFNs to executable codes in Java, Ada, and BPEL have been investigated. Considering readability, extensibility and efficiency of the generated codes, structured translations [2, 10, 13–15, 17] draw much attention. Within structured translations, behavioral constructs, such as sequences, choices, and loops, are mapped into the corresponding structured statements of programming languages. The challenge is that some complex constructs are difficult to be translated into conventional structured statements directly. In the translations from WFNs to BPEL in [2, 15], some complex constructs are mapped to flow activities with control links to indicate the expected execution order. These methods are unsuitable for common programming languages because of the usage of flow statements. In [2], manual translation is employed when a complex construct cannot be translated automatically. There are also other approaches [9, 12, 18, 19] through structured graph-oriented

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models, since the structured translation from structured WFNs to programming languages is smooth. However, it is declared in [12] that there exist WFNs without any equivalent structured models. To sum up, there are still lots of difficulties in the structured transformation from WFNs to programming languages. In addition, most of the existing structured translations just aim at the implementation of WFNs without considering verification of correctness of the models.

Modeling, Simulation and Verification Language (MSVL) [6] is an executable subset of Projection Temporal Logic (PTL) [20]. In addition to common statements, eg, *assignment*, *sequence*, *condition* and *loop*, in C, C++, and Java, etc., concurrent statements like *await*, *parallel*, as well as *projection* are also provided in MSVL. As a modeling, simulation and verification language, MSVL can perform as a programming language for simulation, model a concurrent system like PROMELA [11], and verify critical properties of a system through model checking approaches. Meanwhile, supporting tool for simulation, modeling and verification with MSVL has been well developed [6].

Therefore, we are motivated to implement WFNs with MSVL such that WFNs models can be not only implemented but also verified with properties specified by Propositional Projection Temporal Logic formulas (PPTL) [6]. To the end of the translation from WFNs to MSVL programs, annotations are added to WFNs first. Further, translating rules are presented for the translation from Annotated WFNs (AWFNs) to MSVL programs and a tool called PN2MSVL is implemented for the automatic translation from WFNs to MSVL. The merits of the translation presented in this paper are in two folds: (1) the translation is structured and easy to be extended to other general programming languages; (2) when transformed as MSVL programs, critical properties of the original WFN models can be verified via model checking approaches.

The rest of the paper is organized as follows. Section 2 introduces the notation and the

$\bullet t_1 \cap \bullet t_2 \neq \emptyset$ , then  $\bullet t_1 = \bullet t_2$ . Given a free-choice net  $N$ , a *complete choice* is a maximal subset of transitions with the same input places, and the set of all complete choices is denoted by  $CC_N$ .

In general only the models that have been verified will be useful in practice, and soundness is widely accepted as an essential attribute of well designed models. Further, free-choice nets are an important subclass of Petri nets. As a good compromise between expressive power and analyzability, free-choice nets have strong theoretical results and efficient analysis algorithms [5]. With these considerations, in this paper we only deal with sound free-choice WFNs.

## 2.2 MSVL

MSVL is an executable subset of PTL. Expressions of MSVL are presented below:

$$e ::= n|s|x$$

$$b ::= \text{true}|\text{false}|e_0 = e_1|\neg b|b_0 \text{ and } b_1$$

where  $n$  is an integer,  $s$  a string, and  $x$  a variable. The following are the statements in MSVL:

Assignment :	$x_1 \leq e$	Sequential :	$p_1; p_2$
Conditional :	$\text{if } b_1 \text{ then } \{p_1\} \text{ else } \{p_2\}$	While :	$\text{while } b_1 \text{ do } \{p_1\}$
Guarded Conditional :	$(b_1 \rightarrow p_1)[] \dots [](b_m \rightarrow p_m)$	Selection :	$(p_1)\text{or}(p_2)$
Interval Frame :	$\text{frame}(x_1, \dots, x_n)$	Parallel :	$(p_1)\  (p_2)$
Await :	$\text{await}(b_1)$	Skip :	$\text{skip}$

where  $e$  stands for an arbitrary expression, each  $b_i$  a boolean expression, each  $p_i$  a statement,  $i \in \{1, 2, \dots, m\}$ , and each  $x_j$  a statement of MSVL,  $j \in \{1, 2, \dots, n\}$ .  $x_1 \leq e$  means that the value of variable  $x_1$  is assigned to the value of expression  $e_1$  and a proposition  $p_{x_1}$  combined with  $x_1$ , in the mean time, is set to true. The sequential, conditional, and while statements are the same as that of conventional imperative languages.  $(b_1 \rightarrow p_1)[] \dots [](b_m \rightarrow p_m)$  means that if none of the conditions is true, the program will abort; otherwise an arbitrary program  $p_i$  with a true guard  $b_i$  will be selected for execution.  $(p_1)\text{or}(p_2)$  means that either  $p_1$  or  $p_2$  is executed.  $\text{frame}(x_1, \dots, x_n)$  indicates that for every variable  $x_j$  the value of it keeps unchanged over an interval if no assignment to it is encountered.  $(p_1)\| (p_2)$  means that  $p_1$  and  $p_2$  start simultaneously, execute parallelly, and can end asynchronously.  $\text{await}(b_1)$  does not change any variable, but waits until the condition  $b_1$  becomes true, at which point it terminates.  $\text{skip}$  specifies an interval of unit length.

Currently, a tool named MSV has been developed for MSVL. MSV can work in three modes: simulation, modeling, and verification. In the simulation mode, an MSVL program is executed with an interpreter; in the modeling mode, the whole state space of the program can be illustrated in terms of Normal Form Graph (NFG) [7]; and in the verification mode, a Propositional Projection Temporal Logic (PPTL) formula is used to specify the desired property of the model, then the unified model checking approach [6] is utilized to check whether the MSVL model can satisfy the PPTL formula.

### 3 Annotated Workflow Nets and Regular Structures

For the fluent translation from WFNs to MSVL, we introduce Annotated Workflow Nets (AWFNs) and regular structures in AWFNs first.

#### 3.1 Annotated Workflow Nets

**Definition 2.** An Annotated WFN (AWFN) is a tuple  $(P, T, F, G, L)$ , where  $N = (P, T, F)$  is a WFN,  $G$  and  $L$  are condition and statement annotations on a transition  $t \in T$ , respectively. For each transition  $t \in T$ , the condition annotation  $G(t)$  of  $t$  is a boolean expression, and the statement annotation  $L(t)$  of  $t$  is a statement in MSVL.

In an AWFN, a transition  $t$  is *enabled* iff for each place  $p \in \bullet t$ ,  $M(p) > 0$  and  $G(t)$  is true. The statement annotation  $L(t)$  will be executed while  $t$  is fired. AWFNs serve as an intermediary in the translation from WFNs to MSVL.

Given a sound free-choice WFN  $N = (P, T, F)$ , an AWFN  $AN = (P, T, F, G, L)$  can be obtained by:

- $G(t) = \text{true}$  for each  $t \in T$ ,
- $L(t) = (p_1 \leq 0) \text{ and } \dots \text{ and } (p_m \leq 0) \text{ and skip}; (q_1 \leq 1) \text{ and } \dots \text{ and } (q_n \leq 1) \text{ and skip}$ , where  $\bullet t = \{p_1, \dots, p_m\}$  and  $t^\bullet = \{q_1, \dots, q_n\}$ .

Intuitively, for each place  $p$  of  $N$ , a variable  $p$  is utilized to record the number of tokens in it, and for each transition  $t$ , a statement  $L(t)$  is employed to describe the effect of the transition  $t$  on places.

#### 3.2 Regular Structures

Let  $N = (P, T, F)$  be a Petri net. For two nodes  $x, y \in P \cup T$ , there exists a path from  $x$  to  $y$  iff  $(x, y) \in F^+$ .  $N$  is *standard* iff there exist two distinct nodes, denoted by  $st_N$  and  $end_N$  (means starting and ending node, respectively), such that every node appears on a path from  $st_N$  to  $end_N$ . Let  $X \subseteq P \cup T$  be a set of nodes. The *projection* of  $N$  to  $X$  is a subnet  $N|_X = (P|_X, T|_X, F|_X)$  of  $N$ , where  $P|_X = P \cap X$ ,  $T|_X = T \cap X$ ,  $F|_X = F \cap ((P|_X \times T|_X) \cup (T|_X \times P|_X))$ , and for each node  $x \in X$ ,  $\bullet x|_X = \bullet x \cap X$  and  $x^\bullet|_X = x^\bullet \cap X$ .  $N|_X$  is *autonomous* iff  $N|_X$  is standard,  $(\bullet st_{N|_X} \cup end_{N|_X}^\bullet) \cap X = \emptyset$ , and  $\bullet X' \cup X'^\bullet = X$ , where  $X' = X \setminus \{st_{N|_X}, end_{N|_X}\}$ .

Now given a sound free-choice AWFN  $N = (P, T, F, G, L)$  as well as a set of nodes  $X \subseteq P \cup T$ . Some regular structures in AWFNs are defined as follows:

1. **Redundant Place Structure:**  $N|_X$  is a *redundant place structure (RPS)* iff  $X = \{p_1, p_2\} \subseteq P$ ,  $\bullet p_1 = \bullet p_2$ , and  $p_1^\bullet = p_2^\bullet$ . Fig. 1 (a) shows a RPS, where  $M(q_1) = M(q_2)$  for any reachable marking  $M$ .
2. **Sequence Structure:**  $N|_X$  is a *sequence structure (SS)* iff  $T|_X = \{t_1, t_2\}$ ,  $P|_X = \{p\} = t_1^\bullet = \bullet t_2$ ,  $\bullet p = \{t_1\}$ , and  $p^\bullet = \{t_2\}$ . Obviously, a sequence structure is a standard net. Fig. 2 (a) shows an SS, where  $t_1$  and  $t_2$  always occur sequentially.
3. **Explicit Choice Structure:**  $N|_X$  is an *explicit choice structure (ECS)* iff  $P|_X = P_1 \cup P_2$ ,  $P_1 \cap P_2 = \emptyset$ ,  $|P_1| > 0$ ,  $|P_2| > 0$ ,  $|T|_X| > 1$ , and  $\forall t \in T|_X, \bullet t = P_1, t^\bullet = P_2$ . Fig. 3 (a) shows an ECS, where the occurrences of  $t_1$  and  $t_2$  are mutually exclusive.

4. Simple Loop Structure:  $N|_X$  is a *simple loop structure (SLS)* iff  $T|_X = \{t\}$  and  $P|_X = \bullet t = t^\bullet$ . Fig. 4 (a) shows a SLS, where  $t_0$  can occur repeatedly.
5. Complex Loop Structure:  $N|_X$  is a *complex loop structure (CLS)* iff  $N|_X$  is connected,  $|T|_X| > 1$ ,  $\forall t \in T|_X, |\bullet t| = |t^\bullet| = 1$ , and  $\forall p \in P|_X, |\bullet p|_X| = |p^\bullet|_X| = 1$ . Since  $N$  is a free-choice WFN, we have  $\forall p \in P|_X, \forall t \in p^\bullet, \bullet t = \{p\}$ . The dashed rectangle in Fig. 5 (a) shows a CLS, where once one transition in the loop occurs, all transitions in the loop will occur iteratively.
6. Complex Choice Structure:  $N|_X$  is a *complex choice structure (CCS)* iff  $N|_X$  is a standard net,  $st_{N|_X}, end_{N|_X} \in P|_X, \forall t \in T|_X, |t^\bullet| = |\bullet t| = 1, \forall p \in P|_X \setminus \{st_{N|_X}, end_{N|_X}\}, |p^\bullet|_X| = |\bullet p|_X| = 1, |st_{N|_X}^\bullet|_X| = |\bullet end_{N|_X}|_X| = 2, \bullet st_{N|_X} \neq \emptyset, end_{N|_X}^\bullet \neq \emptyset$ , and  $\forall t \in end_{N|_X}^\bullet, |\bullet t| = 1$ . Similarly, since  $N$  is a free-choice net, for all  $p \in P|_X$  and  $t \in p^\bullet$ , we have  $\bullet t = \{p\}$ . The dashed rectangle in Fig. 6 (a) presents a CCS where four cases:  $t_1$  and  $t_2$ , or  $t_3$  and  $t_4$  fire together, or only  $t_1$  or  $t_4$  fires.
7. Concurrent Structure:  $N|_X$  is a *concurrent structure (CoS)* iff  $N|_X$  is autonomous,  $st_{N|_X}, end_{N|_X} \in T|_X, \forall p \in P|_X, |\bullet p| = |p^\bullet| = 1$ , and  $T|_X = \bullet(P|_X) \cup (P|_X)^\bullet$ . A *minimal CoS* is a CoS where no smaller CoS can be contained. Fig. 7 (a) presents a CoS, where after the occurrence of  $t_0$ , all the rest transitions in it will occur.
8. Irregular Structure:  $N|_X$  is an *irregular structure (IS)* iff  $X$  is autonomous and containing no regular structures defined above. A *minimal IS* is an IS where no smaller IS can be contained. Since  $N$  is a sound net, once a transition in an IS  $N|_X$  occurs, the occurrence of  $N|_X$  will eventually end with no tokens left. Fig. 8 (a) shows an IS where once  $t_0$  or  $t_1$  occurs,  $t_3$  will eventually occur.

## 4 Translation from AWFNs to MSVL

With respect to each regular structure, a translating rule is given for the transformation from AWFNs to the eventually MSVL programs.

### 4.1 Rule RRP: Removal of Redundant Places

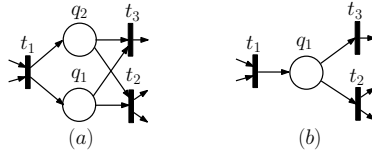
For each reachable marking of a sound free-choice AWFN, the numbers of tokens contained in all places of a redundant place structure are the same. Thus, control-flow of the structure will not be changed in case any one of the places is removed. Accordingly, for a redundant place structure  $N|_X$ , we remove one of the two places in  $X$ .

Formally, for a redundant place structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , by RULE RRP, a new sound free-choice AWFN  $N' = (P', T, F', G, L)$  is obtained, where  $P' = P \setminus \{p\}$ ,  $p \in X$ , and  $F' = (F \cap ((P' \times T) \cup (T \times P')))$ .

As an example, for the redundant place structure illustrated in Fig. 1 (a), by RULE RRP, place  $q_2$  is removed as depicted in Fig. 1 (b).

### 4.2 Rule FSS: Folding Sequence Structures

In a sequence structure, two transitions always occur sequentially. We fold them into one transition with statement annotation being the sequential composition of the two statement annotations on the two transitions.

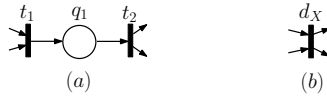


**Fig. 1.** Removal of Redundant Places

Formally, for a sequence structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , by RULE FSS, a new sound free-choice AWFN  $N' = (P', T', F', G', L')$  is generated, where

- $P' = P \setminus X$ ;
- $T' = (T \setminus X) \cup \{d_X\}$ ,  $d_X \notin P \cup T$ ;
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup (\bullet st_{N|_X} \times \{d_X\}) \cup (\{d_X\} \times end_{N|_X} \bullet)$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $G'(t) = G(t)$ , and  $G'(d_X) = G(st_{N|_X})$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $L'(t) = L(t)$ , and  $L'(d_X) = L(st_{N|_X}); L(end_{N|_X})$ .

For instance, by RULE FSS, the sequence structure in Fig. 2 (a) can be transformed as  $d_X$  in Fig. 2 (b) where  $G'(d_X) = G(t_1)$ , and  $L'(d_X) = L(t_1); L(t_2)$ .



**Fig. 2.** Folding Sequence Structures

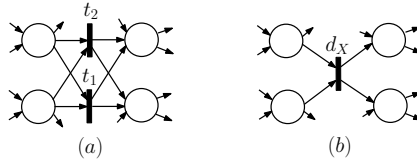
### 4.3 Rule FECS: Folding Explicit Choice Structures

In an explicit choice structure, the occurrences of transitions are mutually exclusive. The transitions are folded into one transition with a guarded conditional statement as the statement annotation.

Formally, for an explicit choice structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , by RULE FECS, a new sound free-choice AWFN  $N' = (P, T', F', G', L')$  is produced, where

- $T' = (T \setminus X) \cup \{d_X\}$ ,  $d_X \notin P \cup T$ ;
- $F' = (F \cap ((P \times T') \cup (T' \times P))) \cup (\bullet(T|_X) \times \{d_X\}) \cup (\{d_X\} \times T|_X \bullet)$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $G'(t) = G(t)$ , and  $G'(d_X) = \text{OR}_{d \in T|_X} G(d)$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $L'(t) = L(t)$ , and  $L'(d_X) = (G(t_0) \rightarrow L(t_0))[] \dots [] G(t_n) \rightarrow L(t_n)$ , where  $T|_X = \{t_0, \dots, t_n\}$ .

For example, by RULE FECS, the explicit choice structure in Fig. 3 (a) is folded as the transition  $d_X$  in Fig. 3 (b) where  $G'(d_X) = G(t_1)$  or  $G(t_2)$  and  $L'(d_X) = (G(t_1) \rightarrow L(t_1))[] (G(t_2) \rightarrow L(t_2))$ .



**Fig. 3.** Folding Explicit Choice Structures

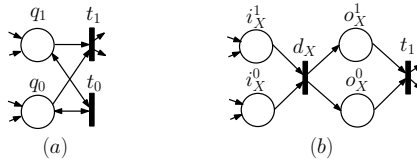
#### 4.4 Rule FSLs: Folding Simple Loop Structures

In a simple loop structure, the transition could occur repeatedly. We fold this structure into one transition with a while statement as the statement annotation.

Formally, for a simple loop structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , by RULE FSLs, a new sound free-choice AWFN  $N' = (P', T', F', G', L')$  is obtained, where

- $P' = (P \setminus X) \cup P_0 \cup P_1$ , where  $P_0 \cap P_1 = \emptyset$ ,  $(P_0 \cup P_1) \cap (P \cup T) = \emptyset$ , and there exist bijective mappings  $\mu_0, P|_X \rightarrow P_0$ , and  $\mu_1, P|_X \rightarrow P_1$ ;
- $T' = (T \setminus X) \cup \{d_X\}$ ,  $d_X \notin P \cup T \cup P_0 \cup P_1$ ;
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup (P_0 \times \{d_X\}) \cup (\{d_X\} \times P_1) \cup F_0 \cup F_1$ , where  $F_0 = \{(x, \mu_0(p)) | \forall p \in P|_X, \forall (x, p) \in F|_X\}$  and  $F_1 = \{(\mu_1(p), x) | \forall p \in P|_X, \forall (p, x) \in F|_X\}$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $G'(t) = G(t)$ , and  $G'(d_X) = \text{true}$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $L'(t) = L(t)$  and  $L'(d_X) = \text{over}_X \leq 0$  and `skip;while(overX = 0 and G(t))`{`overX <= 1 and skip` or  $L(t)$ }, where  $T|_X = \{t\}$ .

For instance, by RULE FSLs, the simple loop structure in Fig. 4 (a) is folded as transition  $d_X$  in Fig. 4 (b), where  $G'(d_X) = \text{true}$  and  $L'(d_X) = \text{over}_X \leq 0$  and `skip;while(overX = 0 and G(t0))`{`overX <= 1 and skip` or  $L(t_0)$ }.



**Fig. 4.** Folding Simple Loop Structures

#### 4.5 Rule FCLS: Folding Complex Loop Structures

In a complex loop structure, whenever a transition occurs, all transitions in it will occur iteratively. Accordingly, we fold a complex loop structure as a transition with a while statement as the statement annotation. Further, since it may have more than one entries or exits, two auxiliary variables  $LPNext_X$  and  $LPOut_X$  are utilized to mark the actual entry and exit in one occurrence.

Let  $N|_X$  be a complex loop structure of a sound free-choice AWFN  $N = (P, T, F, G, L)$ .  $entry_X$  and  $exit_X$  denotes the set of entries and exits of  $N|_X$ , respectively. Formally,  $entry_X = \{p | \forall p \in P|_X, \bullet p \setminus X \neq \emptyset\}$  and  $exit_X = \{p | \forall p \in P|_X, p \bullet \setminus X \neq \emptyset\}$ . Once a transition

in  $N|_X$  with an entry of  $N|_X$  as input place occurs, the occurrence of  $N|_X$  starts. While in case a transition outside of  $N|_X$  with an exit of  $N|_X$  as input place occurs, the occurrence of  $N|_X$  ends. Therefore, when an exit  $q$  of  $N|_X$  gets the token, the occurrence of  $N|_X$  can end if one transition  $d$ , outside of  $N|_X$ , with  $q$  as input is enabled, i.e.  $\text{OR}_{t \in p^* \setminus X} G(t)$  holds. For convenience, we use  $EG_X(p)$  to indicate  $\text{OR}_{t \in p^* \setminus X} G(t)$  for each place  $p$  in  $\text{exit}_X$ . To formally present the details of the transformation, notations below are defined first.

$LN_X \subseteq \text{entry}_X \times \text{entry}_X$  is a binary relation such that for any  $(p_0, p_1) \in LN_X$ , there exists a path in  $N|_X$  from  $p_0$  to  $p_1$  containing no other entries of  $N|_X$ .  $N|_Y$  is a segment of  $N_X$  iff  $Y \subseteq X$ ,  $N|_Y$  is a standard net, and  $(st_{N|_Y}, end_{N|_Y}) \in LN_X$ . Now we extend relation  $LN_X$  to segments, namely segments  $LN_X$  ( $SLN_X$ ). Let  $N|_{Y_1}$  and  $N|_{Y_2}$  be two distinct segments.  $(N|_{Y_1}, N|_{Y_2}) \in SLN_X$  iff  $(st_{N|_{Y_1}}, st_{N|_{Y_2}}) \in LN_X$ . For instance, in the complex loop structure  $N|_X$  illustrated in the dashed rectangle of Fig. 5 (a),  $\text{entry}_X = \{q_1, q_2\}$ ,  $\text{exit}_X = \{q_1, q_3\}$ ,  $EG_X(q_1) = G(t_5)$ ,  $EG_X(q_3) = G(t_7)$ , and  $LN_X = \{(q_1, q_2), (q_2, q_1)\}$ . There are two segments  $N|_{X_1}$  and  $N|_{X_2}$  of loop structure  $N|_X$ , where  $X_1 = \{q_1, q_2, t_0\}$ ,  $X_2 = \{q_2, q_3, q_1, t_1, t_2\}$ , and  $(N|_{X_1}, N|_{X_2}), (N|_{X_2}, N|_{X_1}) \in SLN_X$ .

To construct the statement annotation of the transition formed by RULE FCLS, each segment of a complex structure is mapped into a conditional statement, and then a while statement is constructed such that an arbitrary conditional statement among them serves as the starting, and all conditional statements occur w.r.t to the relations of segments described in  $SLN_X$ .

Specifically, given a complex loop structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , a new sound free-choice AWFN  $N' = (P', T', F', G', L')$  is obtained by RULE FCLS, where

- $P' = (P \setminus X) \cup \{i_X, o_X\}$  with  $\{i_X, o_X\} \cap (P \cup T) = \emptyset$ ;
- $T' = (T \setminus X) \cup \{d_X\}$ , where  $d_X \notin P \cup T \cup \{i_X, o_X\}$ ;
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup ((\bullet \text{entry}_X \setminus X) \times \{i_X\}) \cup \{(i_X, d_X), (d_X, o_X)\} \cup \{o_X\} \times (\text{exit}_X \bullet \setminus X)$ ;
- $G'(t) = G(t)$ , for each  $t \in T' \setminus (\text{exit}_X \bullet \cup \{d_X\})$ ;  $G'(t) = G(t)$  and  $LPOut_X = \text{"p"}$ , for each  $t \in \text{exit}_X \bullet \setminus X$ , where  $\bullet t = \{p\}$ ; and  $G'(d_X) = \text{true}$ ;
- $L'(t) = L(t)$ , for each  $t \in T' \setminus (\bullet \text{entry}_X \cup \text{exit}_X \bullet \cup \{d_X\})$ ,  $L'(t) = L(t)$ ;  $LPNext_X \leq \text{"p"}$  and  $\text{skip}$ , for each  $t \in \bullet \text{entry}_X \setminus X$ , where  $t \bullet \cap X = \{p\}$ ,  $L'(t) = LPOut_X \leq \text{"NULL"}$  and  $\text{skip}$ ;  $L'(t)$ , for each  $t \in \text{exit}_X \bullet \setminus X$ , and  $L'(d_X)$  is shown in Statement Annotation 1.

In Statement Annotation 1, for each segment  $N|_Y$  of  $N|_X$  there exists a conditional statement from line 3 to 16. The condition in line 3 is used to check whether the starting place  $st_{N|_Y}$  of  $N|_Y$  gets a token. If the condition does not hold, the conditional statement is skipped. Otherwise,  $LPNext_X$  is assigned as  $\text{"end}_{N|_Y}$ ", which makes the conditional statement of the subsequent segment executable. Thus, the statement annotation of transition  $t_Y^1$  between  $st_{N|_Y}$  and  $r_Y^1$  is executed subsequently. Here  $r_Y^1$  is the first exit in  $N|_Y$ . When  $r_Y^1$  gets a token, a guarded conditional occurs. In case the assignment statement in line 5 is executed, the occurrence of  $N|_X$  ends and the actual exit of this occurrence is marked by  $LPOut_X$ . Otherwise, the occurrence of  $N|_X$  goes on.  $t_Y^2$  is the transition between  $r_Y^1$  and the successive exit  $r_Y^2$ .  $t_Y^3$  is the transition between  $r_Y^2$  and the subsequent exit.  $r_Y^k$  is the last exit in  $N|_Y$  and  $t_Y^k$  is the transition between  $r_Y^k$  and  $end_{N|_Y}$ . All conditional statements occur w.r.t to the relations of segments described in  $SLN_X$ .



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**Statement Annotation 1.**


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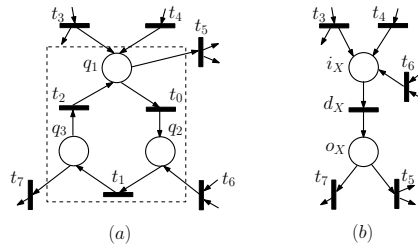
```

1: while( $\neg(LPN_{ext_X} = "NULL")$ ) do{
2:   ...
3:   if( $LPN_{ext_X} = "st_{N|Y}"$ ) then {
4:      $LPN_{ext_X} <= "end_{N|Y}"$  and skip;  $L(t_Y^1)$ ;
5:     ( $EG_X(r_Y^1) \rightarrow LPN_{ext_X} <= "NULL"$  and  $LPOut_X <= "r_Y^1"$  and skip)[]
6:     ( $G(t_Y^2) \rightarrow L(t_Y^2)$ ;
7:      ( $EG_X(r_Y^2) \rightarrow LPN_{ext_X} <= "NULL"$  and  $LPOut_X <= "r_Y^2"$  and skip)[]
8:      ( $G(t_Y^3) \rightarrow L(t_Y^3)$ ;
9:       ...
10:        ( $EG_X(r_Y^k) \rightarrow$ 
11:          $LPN_{ext_X} <= "NULL"$  and  $LPOut_X <= "r_Y^k"$  and skip
12:         )[]( $G(t_Y^v) \rightarrow L(t_Y^v)$ )
13:        ...
14:      )
15:    }
16:  }
17:  ...
18: }
```

---

By RULE FCLS, the complex loop structure shown in Fig. 5 (a) is transformed as  $d_X$  in Fig. 5 (b), where

$G'(t_5) = G(t_5)$  and  $LPOut_X = "q_1"$ ,  $L'(t_5) = LPOut_X <= "NULL"$  and skip;  $L(t_5)$ ,  
 $G'(t_7) = G(t_7)$  and  $LPOut_X = "q_3"$ ,  $L'(t_7) = LPOut_X <= "NULL"$  and skip;  $L(t_7)$ ,  
 $L'(t_3) = L(t_3)$ ;  $LPN_{ext_X} <= "q_1"$  and skip,  
 $L'(t_4) = L(t_4)$ ;  $LPN_{ext_X} <= "q_1"$  and skip,  
 $L'(t_6) = L(t_6)$ ;  $LPN_{ext_X} <= "q_2"$  and skip,  
 $G'(d_X) = \text{true}$ ,  
 $L'(d_X) = \text{while}(\neg(LPN_{ext_X} = "NULL"))$  do{  
   if( $LPN_{ext_X} = "q_1"$ ) then( $LPN_{ext_X} <= "q_2"$  and skip;  
   ( $G(t_5) \rightarrow LPN_{ext_X} <= "NULL"$  and  $LPOut_X <= "q_1"$  and skip)[]( $G(t_0) \rightarrow L(t_0)$ ))  
   if( $LPN_{ext_X} = "q_2"$ ) then( $LPN_{ext_X} <= "q_1"$  and skip;  $L(t_1)$ ;  
   ( $G(t_7) \rightarrow LPN_{ext_X} <= "NULL"$  and  $LPOut_X <= "q_3"$  and skip)[]( $G(t_2) \rightarrow L(t_2)$ ))}



**Fig. 5.** Folding Complex Loop Structures

#### 4.6 Rule FCCS: Folding Complex Choice Structure

We fold a complex choice structure  $N|_X$  as a transition with a conditional statement as the statement annotation. Similar to complex loop structures, there may be more than one entries and exits in a complex choice structure. Thus, two auxiliary variables

$CCNext_X$  and  $CCOut_X$  are utilized to mark the position where an occurrence of  $N|_X$  starts and stops, respectively.

Let  $N|_X$  be a complex choice of a sound free-choice AWFN  $N = (P, T, F, G, L)$ . The definitions of  $entry_X$ ,  $exit_X$ ,  $EG_X$ , and  $LN_X$  are the same as that of complex loop structures.  $N|_Y$  is a *segment* of  $N|_X$  iff  $Y \subset X$ ,  $N|_Y$  is a standard net, and (1)  $(st_{N|_Y}, end_{N|_Y}) \in LN_X$ , or (2)  $Y \cap entry_X = st_{N|_Y}$  and  $end_{N|_Y} = end_{N|_X}$ . Note that among the segments of  $N|_X$ , there are two starting at  $st_{N|_X}$  as well as two ending at  $end_{N|_X}$ . The definition of  $SLN_X$  is the same as that of complex loop structures. For instance, for the complex choice structure  $N|_X$  as shown in the dashed rectangle of Fig. 6 (a),  $entry_X = \{q_0, q_2\}$ ,  $exit_X = \{q_1, q_3\}$ ,  $EG_X(q_1) = G(t_7)$ ,  $EG_X(q_3) = G(t_5)$ ,  $LN_X = \{(q_0, q_2), (q_2, q_3), (q_0, q_3)\}$ . There are three segments  $N|_{X_1}$ ,  $N|_{X_2}$ , and  $N|_{X_3}$  of  $N|_X$ , where  $X_1 = \{q_0, q_2, t_3\}$ ,  $X_2 = \{q_2, q_3, t_4\}$ ,  $X_3 = \{q_0, q_1, q_3, t_1, t_2\}$ , and  $SLN_X = \{(N|_{X_1}, N|_{X_2})\}$ .

According to the definition of complex choice structure  $N|_X$ , there are two different paths from  $st_{N|_X}$  to  $end_{N|_X}$ . To construct the statement annotation of the transition formed by RULE FCCS, (1) for each path from  $st_{N|_X}$  to  $end_{N|_X}$ , a sequential statement is constructed with conditional statements obtained from segments in it; (2) in each sequential statement, all conditional statements occur w.r.t to the relations of segments described in  $SLN_X$ ; and (3) a new guarded conditional statement with these two sequential statements as branches is constructed.

Specifically, given a complex choice structure  $N|_X$  of a sound free-choice AWFN  $N = (P, T, F, G, L)$ , a new sound free-choice AWFN  $N' = (P', T', F', G', L')$  is obtained by RULE FCCS, where

- $P' = (P \setminus X) \cup \{i_X, o_X\}$ , and  $\{i_X, o_X\} \cap (P \cup T) = \emptyset$ ;
- $T' = (T \setminus X) \cup \{d_X\}$ , where  $d_X \notin P \cup T \cup \{i_X, o_X\}$ ;
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup ((\bullet entry_X \setminus X) \times \{i_X\}) \cup \{(i_X, d_X), (d_X, o_X)\} \cup \{o_X\} \times (exit_X \bullet X)$ ;
- $G'(t) = G(t)$ , for each  $t \in T' \setminus (exit_X \bullet \cup \{d_X\})$ ;  $G'(t) = G(t)$  and  $CCOut_X = \text{"p"}$ , for each  $t \in exit_X \bullet X$ , where  $\bullet t = \{p\}$ ; and  $G'(d_X) = \text{true}$ ;
- $L'(t) = L(t)$ , for each  $t \in T' \setminus (\bullet entry_X \cup exit_X \bullet \cup \{d_X\})$ ;  $L'(t) = L(t)$ ;  $CCNext_X \leq \text{"p"}$  and skip, for each  $\forall t \in \bullet entry_X \setminus X$ , where  $t \bullet \cap X = \{p\}$ ;  $L'(t) = CCOut_X \leq \text{"NULL"}$  and skip;  $L(t)$ , for each  $t \in exit_X \bullet X$ ; and  $L'(d_X) =$

1 :  $(CCNext_X = \text{"a}_0\text{" and } (G(t_0) \text{ or } EG_X(a_0)) \text{ or } CCNext_X = \text{"a}_1\text{" or } \dots \text{ or } CCNext_X = \text{"a}_m\text{"} \rightarrow$   
 2 :  $\dots$ )[]  
 3 :  $(CCNext_X = \text{"b}_0\text{" and } (G(t_1) \text{ or } EG_X(b_0)) \text{ or } CCNext_X = \text{"b}_1\text{" or } \dots \text{ or } CCNext_X = \text{"b}_n\text{"} \rightarrow$   
 4 :  $\dots$ )

In  $L'(d_X)$ , each  $a_i$  and  $b_j$ ,  $i \in \{0, 1, \dots, m\}$ ,  $j \in \{0, 1, \dots, n\}$ , is an entry of the complex choice structure appearing in the two pathes from  $st_{N|_X}$  to  $end_{N|_X}$ . Note that  $a_0 = b_0 = st_{N|_X}$ .  $t_0$  and  $t_1$  are the first transitions in the two pathes from  $st_{N|_X}$  to  $end_{N|_X}$ . The two conditions are used to select a path from  $st_{N|_X}$  to  $end_{N|_X}$  for executing. For each segment of a path, in line 2 (or 4) there exists a conditional statement similar to the one from line 3 to 16 in Statement Annotation 1 with  $LPNext_X$  and  $LPOut_X$  being replaced by  $CCNext_X$  and  $CCOut_X$ . All conditional statements in line 2 and 4 occur w.r.t to the relations of segments described in  $SLN_X$ . For segments  $N|_Y$  ending at  $end_{N|_X}$ , the statement  $CCNext_X \leq \text{"end}_{N|_Y}$ " in line 4 of Statement Annotation 1 is replaced by  $CCNext_X \leq \text{"NULL"}$ , and the codes in line 10 and 12 of Statement Annotation 1 are removed.

By RULE FCCS, the complex choice structure in Fig. 6 (a) is transformed as transition  $d_X$  in Fig. 6 (b), where

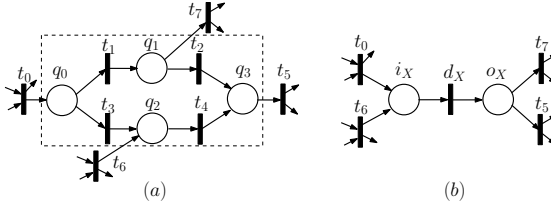
$$\begin{aligned}
 G'(t_5) &= G(t_5) \text{ and } CCOut_X = "q_3", L'(t_5) = CCOut_X \leq "NULL" \text{ and skip}; L(t_5), \\
 G'(t_7) &= G(t_7) \text{ and } CCOut_X = "q_1", L'(t_7) = CCOut_X \leq "NULL" \text{ and skip}; L(t_7), \\
 L'(t_0) &= L(t_0); CCNext_X \leq "q_0" \text{ and skip}, \\
 L'(t_6) &= L(t_6); CCNext_X \leq "q_2" \text{ and skip}, \\
 G'(d_X) &= \text{true}, \\
 L'(d_X) &= (CCNext_X = "q_0" \text{ and } G(t_1) \rightarrow \\
 &\quad \text{if}(CCNext_X = "q_0") \text{ then } \{CCNext_X \leq "NULL" \text{ and skip}; L(t_1); \\
 &\quad \quad (G(t_7) \rightarrow CCNext_X \leq "NULL" \text{ and } CCOut_X \leq "q_1" \text{ and skip})[] \\
 &\quad \quad (G(t_2) \rightarrow L(t_2); CCNext_X \leq "NULL" \text{ and } CCOut_X \leq "q_3" \text{ and skip})[] \\
 &\quad (CCNext_X = "q_0" \text{ and } G(t_3) \text{ or } CCNext_X = "q_2" \rightarrow \\
 &\quad \quad \text{if}(CCNext_X = "q_0") \text{ then } \{CCNext_X \leq "q_2" \text{ and skip}; L(t_3); \\
 &\quad \quad \text{if}(CCNext_X = "q_2") \text{ then } \{L(t_4); CCNext_X \leq "NULL" \text{ and } CCOut_X \leq "q_3" \text{ and skip}\})
 \end{aligned}$$


Fig. 6. Folding Complex Choice Structures

#### 4.7 Rule FCoS: Folding Concurrent Structure

In a concurrent structure  $N|_X$ , once a transition  $st_{N|_X}$  occurs, all other transitions will occur. Thus, it is folded into a transition with a parallel statement as the statement annotation. Furthermore, auxiliary variables and await statements are needed to control the occurrence order of transitions in it.

Given a sound free-choice AWFN  $N = (P, T, F, G, L)$  with a minimal concurrent structure  $N|_X$ , for each  $t \in T|_X$ ,  $B_X(t)$  is used to indicate  $L(t)$ ;  $(B_X(t_1) || \dots || B_X(t_m))$ , where  $\{t_1, \dots, t_m\} = t^{\bullet} \cap (T|_X \setminus \{end_{N|_X}\})$ . We first update  $L(t)$  as  $\text{await}(vp_1 = 1 \text{ and } \dots \text{ and } vp_m = 1); vp_1 \leq 0 \text{ and } \dots \text{ and } vp_m \leq 0 \text{ and skip}; L(t)$ , for each transition  $t \in T|_X \setminus \{st_{N|_X}, end_{N|_X}\}$  with  $|\bullet t| > 1$ , where  $\{p_1, \dots, p_m\} = \bullet t \setminus \{p\}$ ,  $p \in \bullet t$ , and remove input arcs of  $t$  excepting for  $(p, t)$ . Secondly, for each transition  $t \in T|_X$  with  $\exists q \in t^{\bullet}$ ,  $q^{\bullet} = \emptyset$ , we update  $L(t)$  as  $L(t); vq_1 \leq 1 \text{ and } \dots \text{ and } vq_n \leq 1 \text{ and skip}$ , where  $\{q_1, \dots, q_n\} = \{q | \forall q \in t^{\bullet}, q^{\bullet} = \emptyset\}$ . Then it has  $\forall t \in T|_X \setminus \{st_{N|_X}, end_{N|_X}\}, |\bullet t| = 1$ . Finally, we fold  $N|_X$  and generate a new sound free-choice AWFN  $N' = (P', T', F', G', L')$ , where

- $P' = (P \setminus X) \cup \{i_X, o_X\}, \{i_X, o_X\} \cap (P \cup T) = \emptyset$ ;
- $T' = (T \setminus (X \setminus \{st_{N|_X}, end_{N|_X}\})) \cup \{d_X\}, d_X \notin P \cup T \cup \{i_X, o_X\}$ ;
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup \{(st_{N|_X}, i_X), (i_X, d_X), (d_X, o_X), (o_X, end_{N|_X})\}$ ;
- $\forall t \in T' \setminus \{d_X\}, G'(t) = G(t)$ , and  $G'(d_X) = \text{true}$ ;
- $\forall t \in T' \setminus \{d_X\}, L'(t) = L(t)$ , and  $L'(d_X) = \text{frame}(vr_1, \dots, vr_i)$  and  $vr_1 \leq 0$  and  $\dots$  and  $vr_i \leq 0$  and  $((B_X(t_1) || \dots || B_X(t_n)))$ . Note that  $\{t_1, \dots, t_n\} \subseteq T|_X$  are the transitions that still have input places formed by output places of  $st_{N|_X}$  after the first step.  $vr_1, \dots, vr_i$  are the auxiliary variables added in the rule.

By RULE FCoS, the concurrent structure in Fig. 7 (a) is transformed as transition  $d_X$  in Fig. 7 (b), where  $G'(d_X) = \text{true}$  and  $L'(d_X) = \text{frame}(vq_4)$  and  $vq_4 \leq 0$  and  $((L(t_1); (L(t_3) \parallel (\text{await}(vq_4 = 1); vq_4 \leq 0 \text{ and skip}; L(t_4)))) \parallel (L(t_2); vq_4 \leq 1 \text{ and skip}))$ .

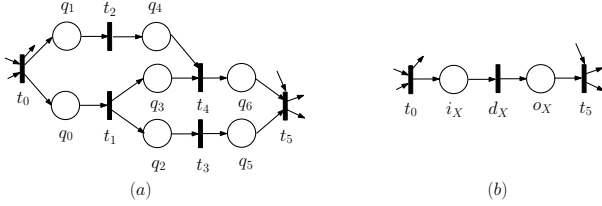


Fig. 7. Folding Concurrent Structures

#### 4.8 Rule FIS: Folding Irregular Structures

In an irregular structure  $N|_X$ , once a transition occurs, the occurrence of  $N|_X$  will eventually ends with no tokens left. Although the control-flow of an irregular structure is complicated, it could still be folded as a transition with a parallel statement as the statement annotation, where the occurring order of the transitions is organized by auxiliary variables and await statements.

Let  $N|_X$  be an irregular structure in a sound free-choice AWFN  $N = (P, T, F, G, L)$ . We define  $stp_X = \{st_{N|_X}\} \cap P$ ,  $endp_X = \{end_{N|_X}\} \cap P$ ,  $stt_X = \{st_{N|_X}\} \cap T$ , and  $endt_X = \{end_{N|_X}\} \cap T$ . Let  $N|_X$  be a minimal irregular structure of  $N$ . We first add an auxiliary transition  $t_{over}$  to  $N$  such that  $t_{over} \bullet = \emptyset$ ,  $L(t_{over}) = over_X \leq 1$  and skip,  $\bullet t_{over} = \bullet end_{N|_X} \cap X$  and  $G(t_{over}) = G(end_{N|_X})$  if  $endt_X \neq \emptyset$ ,  $\bullet t_{over} = \{end_{N|_X}\}$  and  $G(t_{over}) = \text{OR}_{t \in end_{N|_X}} \bullet_X G(t)$  otherwise. Accordingly, a new sound free-choice AWFN  $N' = (P', T', F', G', L')$  is obtained where,

- $P' = (P \setminus X) \cup \{i_X, o_X\}$ ,  $\{i_X, o_X\} \cap (P \cup T \cup \{t_{over}\}) = \emptyset$ ,
- $T' = (T \setminus ((X \cup \{t_{over}\}) \setminus (stt_X \cup endt_X))) \cup \{d_X\}$ ,  $d_X \notin P \cup T \cup \{t_{over}, i_X, o_X\}$ ,
- $F' = (F \cap ((P' \times T') \cup (T' \times P'))) \cup \{(i_X, d_X), (d_X, o_X)\} \cup F_i \cup F_o$ , where  $F_i = (\bullet stp_X \times \{i_X\}) \cup (\{i_X\} \times (stp_X \bullet \setminus X))$ , if  $stp_X \neq \emptyset$ , otherwise  $F_i = stt_X \times \{i_X\}$ ;  $F_o = ((\bullet endp_X \setminus X) \times \{o_X\}) \cup (\{o_X\} \times endp_X \bullet)$ , if  $endp_X \neq \emptyset$ , otherwise  $F_o = \{o_X\} \times endt_X$ ;
- $G'(t) = G(t)$ , for each  $t \in T' \setminus \{d_X\}$ ;  $G'(d_X) = \text{true}$ , if  $stp_X = \emptyset$ , otherwise,  $G'(d_X) = \text{OR}_{d \in stp_X} \bullet_X G(d)$ ;
- $\forall t \in T' \setminus \{d_X\}$ ,  $L'(t) = L(t)$ , and  $L'(d_X) =$

```

...
pro D() = {
  while(over_X = 0){await(vr_1 = 1 and ... and vr_i = 1 or over_X = 1);
    if(over_X = 0) then{vr_1 <= 0 and ... and vr_i <= 0 and skip;
      (G(t_1) → L(t_1); vs_1 <= 1 and ... and vs_j_1 <= 1 and skip)}]
    ...
    [(G(t_k) → L(t_k); vs_k <= 1 and ... and vs_j_k <= 1 and skip)}];
  ...
define start_X() = {vp_j_1 <= 1 and ... and vp_j_k <= 1 and skip};
define end_X() = {over_X <= 0 and skip};
frame(vp_1, ..., vp_n, over_X) and vp_1 <= 0 and ... and vp_n <= 0 and over_X <= 0 and
(start_X(); (D_X^1 || ... || D_X^k); end_X())

```

In  $L'(d_X)$ , for each place  $p \in P|_X$ , an auxiliary variable  $vp$  is used to record the tokens in it. And  $st_{N|X}^* = \{p_{j_1}, \dots, p_{j_k}\}$ , if  $stt_X \neq \emptyset$ , otherwise  $k = 1$  and  $p_{j_1} = st_{N|X}$ . For each complete choice  $\{t_1, \dots, t_k\} = D \in CC_{N|X} = \{D_X^1, \dots, D_X^h\}$ , there exists a process  $D()$  containing a while statement where transitions in  $D$  are executed repeatedly. In a complete choice  $D$ , all transitions have  $\{r_1, \dots, r_i\}$  as input. Thus, all of the transitions have to wait until  $N|_X$  ends or each common input place gets a token. Once one of the transitions occurs, all tokens in the input are consumed, and each output place gets a token.

By RULE FIS, the irregular structure in Fig. 8 (a) is transformed as a transition in Fig. 8 (b), where  $G'(d_X) = \text{true}$  and  $L'(d_X) =$

```

pro  $D_X^1() = \{$ 
  while( $over_X = 0$ ) {await( $vq_1 = 1$  and  $vq_2 = 1$  or  $over_X = 1$ );
    if( $over_X = 0$ ) then { $vq_1 \leq 0$  and  $vq_2 \leq 0$  and skip:( $G(t_3) \rightarrow over_X \leq 1$  and skip)}};
pro  $D_X^2() = \{$ 
  while( $over_X = 0$ ) {await( $vq_3 = 1$  or  $over_X = 1$ );
    if( $over_X = 0$ ) then { $vq_3 \leq 0$  and skip:( $G(t_2) \rightarrow L(t_2); vq_1 \leq 1$  and skip)}};
pro  $D_X^3() = \{$ 
  while( $over_X = 0$ ) {await( $vq_0 = 1$  or  $over_X = 1$ );
    if( $over_X = 0$ ) then { $vq_0 \leq 0$  and skip;
      ( $G(t_0) \rightarrow L(t_0); vq_1 \leq 1$  and  $vq_2 \leq 1$  and skip)[
      ( $G(t_1) \rightarrow L(t_1); vq_2 \leq 1$  and  $vq_3 \leq 1$  and skip)}};
define  $start_X() = \{vq_0 \leq 1$  and skip;
define  $end_X() = \{over_X \leq 0$  and skip;
frame( $vq_3, vq_2, vq_1, vq_0, over_X$ ) and  $vq_3 \leq 0$  and  $vq_2 \leq 0$  and  $vq_1 \leq 0$  and  $vq_0 \leq 0$ 
and  $over_X \leq 0$  and ( $start_X()$ ;  $D_X^1()$  ||  $D_X^2()$  ||  $D_X^3()$ ;  $end_X()$ )
    
```

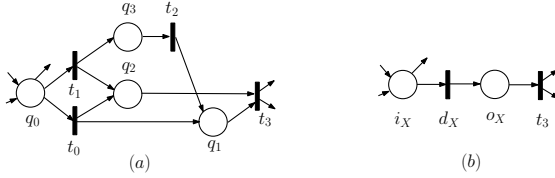


Fig. 8. Folding Irregular Structures

## 4.9 Translation Algorithm

Based on the translating rules, Algorithm PN2MSVL is presented for the translation from sound free-choice WFNs to MSVL programs.

In the MSVL program generated by Algorithm PN2MSVL, for each place  $p_h \in P = \{p_1, \dots, p_a\}$ , a variable  $p_h$  is introduced in the final MSVL program. Especially,  $p_1$  specifies the source place of  $N$ .  $v_1, \dots, v_b$  are the extra variables introduced by translating rules where  $v_i^1, \dots, v_i^j$  (or  $v_s^1, \dots, v_s^k$ ) are all integer (string) variables among them. For each transition  $t$  of  $T$  there exists a definition statement, where  $\bullet t = \{p_t^1, \dots, p_t^m\}$  and  $t^\bullet = \{q_t^1, \dots, q_t^n\}$ .

<b>Algorithm PN2MSVL:</b>
<i>Translation from sound free-choice WFNs to MSVL programs</i>
<b>Input:</b> A sound free-choice WFN $N = (P, T, F)$ ;
<b>Output:</b> A MSVL program;
Translate $N$ to the corresponding AWFN $AN = (P, T, F, G, L)$ ;
<b>while</b> $ T  > 1$
<b>if</b> $AN$ has a redundant place structure <b>then</b> Apply <b>RULE RRP</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has a sequence structure <b>then</b> Apply <b>RULE FSS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has an explicit choice structure <b>then</b> Apply <b>RULE FECS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has a simple loop structure <b>then</b> Apply <b>RULE FSLS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has a complex loop structure <b>then</b> Apply <b>RULE FCLS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has a complex choice structure <b>then</b> Apply <b>RULE FCCS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has a concurrent structure <b>then</b> Apply <b>RULE FCoS</b> to $AN$ ; <b>continue</b> ;
<b>if</b> $AN$ has an irregular structure <b>then</b> Apply <b>RULE FIS</b> to $AN$ ; <b>continue</b> ;
Add initialization, frame and definition statements to $L(t)$ ; <span style="float: right;">/* Let <math>T = \{d\}</math> */</span>
<b>return</b> the final MSVL program shown as follows.
frame( $p_1, \dots, p_a, v_1, \dots, v_b$ ) and $p_1 \leq 1$ and $p_2 \leq 0$ and ... and $p_a \leq 0$ and
$v_i^1 \leq 0$ and ... and $v_i^j \leq 0$ and $v_s^1 \leq \text{"NULL"}$ and ... and $v_s^k \leq \text{"NULL"}$ and (
define $t() = (p_i^1 \leq 0$ and ... and $p_i^m \leq 0$ and skip;
$q_i^1 \leq 1$ and ... and $q_i^l \leq 1$ and skip);
...
$L(d)$

### 5 Experiments

We have realized Algorithm PN2MSVL as a tool named PN2MSVL (<http://ictt.xidian.edu.cn/toolkit/>). PN2MSVL gets a WFN in .g format that can be produced by Workcraft [21] and outputs an MSVL program.

For the sound free-choice WFN in Fig. 9, a MSVL program can be obtained by PN2MSVL as below.

```

frame( $p_9, p_8, p_7, p_6, p_5, p_4, p_3, p_2, p_1, p_0, LPNext0, LPOut0$ ) and  $p_0 \leq 1$  and  $p_9 \leq 0$ 
and  $p_8 \leq 0$  and  $p_7 \leq 0$  and  $p_6 \leq 0$  and  $p_5 \leq 0$  and  $p_4 \leq 0$  and  $p_3 \leq 0$  and  $p_2 \leq 0$ 
and  $p_1 \leq 0$  and  $LPNext0 \leq \text{"NULL"}$  and  $LPOut0 \leq \text{"NULL"}$  and (
define  $t8() = (p_8 \leq 0$  and  $p_6 \leq 0$  and skip;  $p_9 \leq 1$  and skip);
...
 $t0()$ ;
frame( $vp7$ ) and  $vp7 \leq 0$  and (
(await( $vp7 = 1$ );  $vp7 \leq 0$  and skip;  $t6()$ ))|
(
(true  $\rightarrow t5()$ ;  $LPNext0 \leq \text{"p4"}$  and skip)|( $true \rightarrow t1()$ ;  $LPNext0 \leq \text{"p3"}$  and skip);
while( $-(LPNext0 = \text{"NULL"})$ ){
if( $LPNext0 = \text{"p3"}$ )then( $LPNext0 \leq \text{"p4"}$  and skip;  $t2()$ )
if( $LPNext0 = \text{"p4"}$ )then( $LPNext0 \leq \text{"p3"}$  and skip;  $t3()$ ;
(true  $\rightarrow LPNext0 \leq \text{"NULL"}$  and  $LPOut0 \leq \text{"p5"}$  and skip)|( $true \rightarrow t7()$ ));
LPOut0  $\leq \text{"NULL"}$  and skip;  $t4()$ ;  $vp7 \leq 1$  and skip));
 $t8()$ 

```

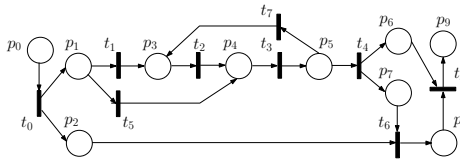


Fig. 9. A Workflow net

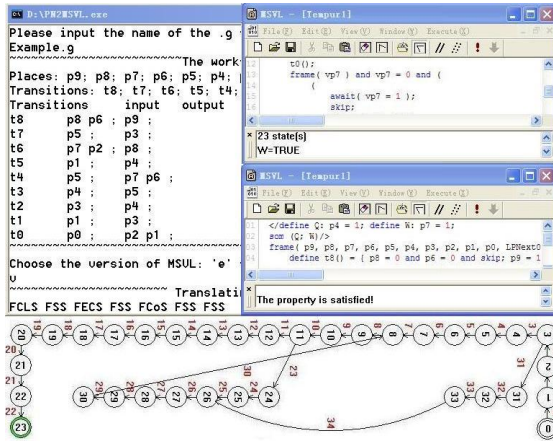


Fig. 10. Results in MSV

When implementing the MSVL program above within MSV, simulation result can be obtained as depicted in the upper right of Fig. 10, where  $W = \text{true}$  means a successful execution of this program. Now we specify the desired property of the model in PPTL:

$$\diamond(Q; W)$$

where  $Q$  and  $W$  means  $p4 = 1$  and  $p7 = 1$ , respectively. The intuition of the formula is that if  $p4 = 1$  holds sometimes,  $p7 = 1$  will holds eventually. The verification result is shown in the lower right of Fig. 10. In addition, the model of the MSVL program can also be explored as illustrated at the bottom of Fig. 10.

## 6 Conclusion

An automatic translation from WFNs to MSVL is presented in this paper. The translation is structured and easy to be extended to other general programming languages. In the near future, we are going to further prove the completeness as well as the soundness of the translation. Also, we will try to improve readability of the generated MSVL programs by exploring more regular structures in AWFNs. As applications, we will translate some big systems modeled by WFNs to MSVL and verify the correctness of these systems with MSV.

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